

# Fragmentation of Production: New Challenges for Big Data—A Complex Network Approach

Giulia De Masi<sup>1</sup> and Giorgio Ricchiuti<sup>2</sup>

<sup>1</sup>Zayed University, Dubai, UAE

<sup>2</sup>Università degli Studi di Firenze, Complexity Lab for Economics, Florence, Italy

Email: giuliademasi@gmail.com, giorgio.ricchiuti@unifi.it

**Abstract**—Globalization is one of the most relevant economic phenomena of the last decades. Due to this reason, the economies of different countries are strongly interconnected. This may lead to higher robustness or higher vulnerability of the whole economic system, depending on the economic scenario. Traditional models are unable to represent the complex relationship among firms. This may lead to a misunderstanding of the complex interconnections between countries, underestimating vulnerability of the world economic system. In this framework, a complex network approach, based on graph theory, is a valuable tool to outline the interdependencies of different countries and their impact on the stability of the whole economic system. Nowadays economic Big Data are available on globalization, helping to have a rigorous approach when shading light on these interdependencies. In this paper, the complex network analysis is applied on a particular shade of globalization, namely fragmentation of production.

**Index Terms**—Complex networks; big data; foreign direct investments

## I. INTRODUCTION

In the last decades, one of the main emerging economic phenomena has been fragmentation of production (the so called globalization) driven by rapidly growing World Wide Web and intercontinental transportation easiness. Globalization has been a relevant opportunity, allowing economic growth toward new markets of enterprises before working only at local/national level. On the other hand, the main risk of global interconnections is related to economic crisis spreading from one country to another through the complex set of economic interdependencies. The larger number of firms engaged in international activities such as exports, FDI and global outsourcing shows that there is a strong heterogeneity in internationally oriented strategies. At the same time, these strategies are strictly connected. This deserves a detailed analysis to better guide the development of the next strategies. It is evident that economic systems have to be represented considering this complex set of connections. Fortunately, nowadays, large databases of economic data (ultimately economic Big Data) are available. For this reason, methods from Big Data literature are applied also

to economic field [1]. Traditional statistics, based on characteristic measurements (like distributions, with their average quantities and their standard deviations), as well as techniques from Machine Learning (like neural networks as other supervised learning algorithms, decision trees and Bayesian statistics) are not enough to investigate a highly interconnected economic system, that can be affected much more severely by internal interconnections than by the behavior of single individuals. Other instruments are necessary. In order to represent and analyze these linkages, it is particularly useful a modeling approach based on complex networks [2]. This approach is scalable and therefore can be extended to big global databases.

Mainstream Economics usually neglect the role of heterogeneity between agents (firms) and their complex interconnections. Only recently some interest rose up on the role of heterogeneity with the decision to export and/or to fragment the production investing in abroad. The network representation allows to identify the role of heterogeneity in order to better understand the long-run economic trend and properly design policy strategies to limit the possible adverse effects on the economic system, particularly in terms of employment.

Complex Network theory is a relatively new field, borderline between different disciplines: particularly Statistical Physics, Mathematics (Graph Theory) and Statistics. In the last decade, it has been set up as a cutting-edge research field in various disciplines of natural sciences (Physics and Biology) and Social Sciences [3]. Networks allow to detect the links and their evolution between different individuals / agents / businesses. In particular, several studies have been carried out to understand the mechanisms underlying communication networks: Internet, World Wide Web (WWW) and e-mail networks. These communication networks are a mirror of the underlying social network, composed of a group of agents who collaborate and compete with each other, gaining mutual benefits from interaction. This approach is promising for the study of economic systems, in which businesses, families, individuals, the State actively interact and shape seamlessly socio-economic structures. The study of

networks is able to reproduce with simple, stylized and meaningful models both stationary and dynamic systems.

The complex network theory, whose mathematical formulation is based on the most well-established theory of graphs, has only recently been applied to Economics [4], allowing to identify and evaluate the structures underlying the relationships between different economic units. Moreover, it allows studying effects that cannot be captured with simple descriptive statistics. Empirical use is mostly related to the structure of the interbank market [5], bank-firm credit market [6], [7], financial market investments [8] and the world trade network [9]. Finally, in literature few studies can be found of the network structure of FDI at global level. The network of the top 100 global multinational and ownership linkages in more than 2000 cities worldwide has been analyzed distinguishing between all industrial sectors and producer service sector [10]. More recently, a worldwide database of multinationals has been analyzed using measurements of network density to study agglomeration phenomena [11]. Relatively to European countries, network based analyses have been done on Italian foreign investment data [12] and on French data [13]. Specifically, De Masi et al. [11] reconstruct the network of Italian firms that invest abroad, showing that even within the same sector, firms can adopt different strategies: horizontal FDI are done by firms that use middle-large countries (Brazil) as a productive platform to export in neighboring through commercial affiliates (the rest of Latin America countries); other firms are global players (vertical FDI), and their production is carried out for cost-saving reasons (in the textile sector), and/or in search of professional skills (if there are machinery producers); finally, they show that there is a strong complementarity between FDI and exports because most of Italian FDI's present commercial purposes. Similarly to [14], in this paper, we reconstruct the network of the European (EU28) firms investing abroad in order to shed light on the role of heterogeneity in the big database of European Foreign Direct Investments. A bipartite network is defined where nodes are investors and their countries of investment. Here the objective of the paper is to identify if investors share similar strategies (in particular which countries they choose to invest) and if more than one strategy emerge within the same economic sector. To this aim, Network analysis is particularly useful, because it allows to represent common investing behavior of firms. In this paper, we assume that if firms have in common both the sector of the parent company and the country of destination, they adopt the same internationalization strategy for foreign direct investment. In particular, we focus on the analysis of sub-structures within the network. The community detection inside the sectoral network allows to investigate the aggregated behavior of subsets of investors and common investment strategies shared within a group of investors, differently from other groups. The analysis is carried out highlighting, at a particular sector level (Industrial Machinery), the evolution of network's

structure and sub-structures, looking to 2003 and 2015 (first and last years of the available dataset), in terms of both countries of destination and activities of the main nodes. The globalization effect is very relevant as evident from the analysis of the two projected networks.

## II. METHODOLOGY

Network analysis allows investigating the topological properties of the complex structure of economic relationships. A network is represented as graph, which is a set of nodes and links.

From a mathematical point of view, a network is represented by an adjacency matrix. The element of the adjacency matrix  $a_{ij}$  indicates that a link exists between nodes  $i$  and  $j$ .

### A. Bipartite Network

In this paper, a bipartite network is defined. A network is called bipartite when two kinds of nodes are present, in our case investing firms and countries. From a mathematical perspective, distinguishing two kinds of nodes, namely  $C$  (countries) and  $I$  (investors), the graph  $G\{C+I\}$ , with a total set of nodes ( $C+I$ ) is defined. A link is drawn if a firm invests in a specific host country, therefore  $a_{ij}=1$  if investor  $i$  goes to country  $j$ ; otherwise  $a_{ij}=0$ .

As an example, a simplified example of a bipartite network of countries and firms is plotted in Fig.1.

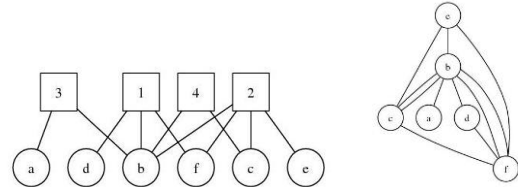


Fig. 1. Bipartition process. Top panel: bipartite graph, considering the set of investors (circles)  $I=\{1,2,3,4\}$  and countries  $C=\{a,b,c,d,e,f\}$  (squares). Bottom panel: corresponding projected graph on firm space.

### B. Projected network

In the study of bipartite graph, a widely used approach is to study separately two networks defined from the original one. In particular, we extract from the overall graph two graphs, each one composed by just one kind of nodes. These two networks are called projected networks, in the sense that they are obtained as a projection of the initial graph in the subspace composed by nodes only of the same kind.

Two new networks are defined,  $G_C$  and  $G_I$ , which have only nodes of kind  $C$  (countries) or  $I$  (investors) respectively.

In Fig. 1, starting from the bipartite network in the left panel, the network projected into the subspace of firms is plotted in the right panel.

In fact, we define weighted networks: the weight of the link between two countries represents the number of firms investing on both of them. On the other hand, the weight of the link between two firms represents the number of common countries they choose.

### C. Topological Measurements

Topological measurements allow understanding different roles of different nodes in the network of firms or network of countries. The most connected nodes are called *hubs* of the network. From an economic perspective, the hub is an economic leader. In the network of firms for instance, a highly connected hub is also usually very central firm which has a varied strategy and shares different strategies with different firms. Therefore, it is a driver and its behavior may affect the behavior of small players like small firms. In this sense, a hub can be considered an economic leader. The less connected nodes can be considered the followers in investing activities.

Different measurements have been considered in this work. The *degree* ( $k$ ) of a node  $i$  is the number of its links to neighbor nodes. This is a measure of node importance and centrality. For weighted networks, also the *weighted degree*  $w$  of a node  $i$  is defined, as the sum of the weights of all its links. The *clustering coefficient* ( $cc1$ ) of a node  $i$  is the number of links between the first neighbors of a node properly normalized to the possible number of links. The *clustering coefficient* ( $cc2$ ) of a node  $i$  looks to the number of links between the first and second neighborhoods of the node. To measure the 'centrality' of a node, many definitions have been given in network analysis, usually based on the concept of distance from other nodes. We use different measures in order to detect the hubs, i.e. the most connected firms within the Industrial Machinery sector and the most connected countries at world level. The *distance* between two vertices is defined as the shortest path (i.e. the lowest number of edges) to go from  $i$  to  $j$ . A first measure of centrality is *degree centrality*, defined as  $dc_i = k_i / (N-1)$ .

The second definition is based on dynamical properties of the graph and is given by the number of times that one vertex  $k$  is crossed by minimal path from one vertex  $i$  to  $j$  (also called distance  $d_{ij}$ ).

This quantity is called *betweenness centrality*  $b_i$  and is usually defined as

$$b_i = \sum_{j,l=1, l \neq j \neq l}^N \frac{d_{jl}(i)}{d_{jl}}$$

where  $d_{jl}$  is the total number of different shortest paths (distances) going from  $j$  to  $l$  and  $d_{jl}(i)$  is the subset of those distances passing through  $i$  [14].

Another measure of centrality is the *closeness centrality*:

$$cl_i = \frac{N-1}{\sum d_{ij}} = \frac{1}{\bar{d}_i}$$

which is the reciprocal of the average distance from that node  $i$  to the other ones [16]. The three measures are related to each other. For example, firms with higher betweenness are also hubs (nodes with high degree centrality). Indeed, in order to minimize the distance, other firms should necessarily pass through a specific

node (a firm). This means that the latter invests in many countries, sharing its own strategy with many other firms. It has a high betweenness and it is a hub.

Most relevantly, subnetworks and communities' detection is a very active field of research. Different methods have been investigated for this work. Here the subnetworks are identified by the  $k$ -core method [17]: the definition of  $k$ -core is a subnetwork of a given network where each network has at least  $k$  neighbors in the same core. In fact,  $k$ -core are set of nodes more connected to each other than with the rest of the nodes of the large network. These tightly connected nodes are also said to form a cluster. This technique allows to identify clusters within a network.

### D. Network Visualization

The visualization of a graph is a crucial point in the study of a network. The study of automatic drawing is a very active field of research. The aim is to obtain a way to represent in the Euclidean space an object (the graph) which is defined only on the topological space. Many algorithms have been proposed. Among them, the Kamada-Kawai algorithm [18] is based on the idea that the suitable geometric distance between two vertices represents the topological distance between them in the graph. The network is represented like a set of particles (nodes) connected by springs. The final network visualization is based on the minimization of the energy associated to this set of coupled harmonic oscillators. This approach allows representing close to each other nodes pertaining to the same group (connected by many links).

The visualization process is certainly a first hint to identify common strategies (if any) between different investors. The Kamada-Kawai layout algorithm indeed allows disclosing the presence of highly clusterized nodes and lowly clusterized or even isolated nodes. The evidence of high clustering shows common strategies between those nodes: they tend to invest in the same countries. On the other hand, low clustering and isolation of a particular node is an evidence of a singular strategy of that node, different from those of other nodes.

## III. DATASET

The dataset is drawn from fDi Markets-Financial Times business, which is a global database of greenfield foreign direct investment (FDI) information. Since 2003, it allows real-time monitoring of FDI projects across all sectors and classified by business function, and it has globally tracked over \$10\$ trillions of investments from over \$80,000\$ companies.

It also includes capital investments and job creation, by tracking and profiling companies investing overseas. To enrich the database, the Financial Times uses different sources: media, project data from industry organizations, information from investment agencies, and data captured from official publication of the companies. In order to validate the data recorded, each project is cross-referenced

through multiple sources. Different scholars have already employed data on FDI markets, to our knowledge none of them have reconstructed a network of European FDI. For the purpose of this paper, our database comprises outward FDI from each of EU28 (countries of origin) to the rest of the world. Therefore, the countries of destination may be also within the EU28 itself. We employ only data for 2003 and 2015 in order to compare the possible change of the FDI-network, due to the crises. While a comparison between different sectors is under study, in this paper we focus on Industrial Machinery sector. This sector presents the largest number of investing and affiliated companies. Moreover, this number increases between the two periods, both investors and affiliates triple in the period from 2003 to 2015, showing a very strong effect of globalization.

#### IV. RESULTS

In order to define the network, a bipartite graph has been generated, where the nodes are both investors and host countries, and a link is drawn if a parent company invests in a certain host country. Projecting the links on two subspaces, two new projected networks are obtained: the network of investors, and the network of countries.

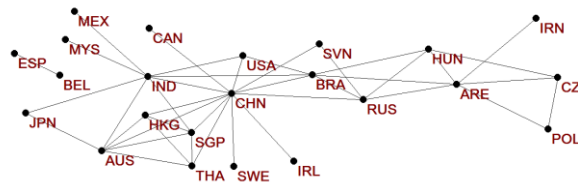


Fig. 2. Projected network on country space (year 2003)

In Fig. 2 and Fig. 3, the country networks for year 2003 and 2015 are reported respectively. It is very evident the large increase of number of countries of investment. This may be due to several factors, especially integration of EU countries and enlargement to the Eastern Europe countries of 2004 and 2007, driving further foreign direct investments also towards new countries.

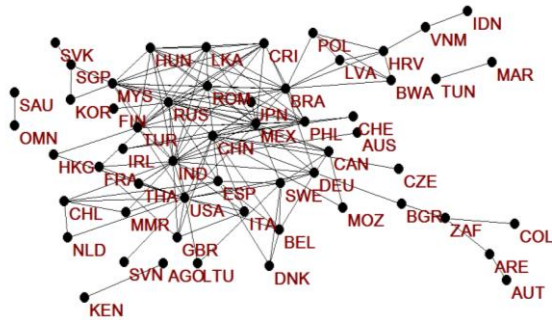


Fig. 3. Projected network on Country space (year 2015)

Main hubs are almost the same, namely China, USA, India, but several new countries appear from far East, Arabian countries and Africa. Two interesting trends can be glimpsed: on the one hand, there is a lower presence of Eastern European countries replaced by new countries of destination (India, Turkey for example), on the other there is an increase in projects in the key hubs of EU28. Rather

than cost reduction, companies in the mechanical industry seem to be interested in workers' skills and the concentration of specific region of production within the same union. This could support the so-called phenomenon of near-shoring, that is the tendency to expand business in nearby countries, more than to far away countries. More in-depth response may be given by the analysis of the evolution of the network that will be done in a future work.

TABLE I. TOPOLOGICAL MEASUREMENTS FOR INVESTOR NETWORK

	Year	
	2003	2015
<i>Investors</i>	101	323
<i>Countries</i>	23	67
<i>k</i>	0.7	2.2
<i>w</i>	6.1	1.3
<i>cc1</i>	6.7	6.6
<i>cc2</i>	1.5	4.2
<i>b</i>	6.3	8.7
<i>cl</i>	3.9	2.0

In Table I the comparison of the most relevant above described topological measurements on investor networks between the two selected years (2003 and 2015) are reported. The total number of investors and countries of investment is tripled. The average degree ( $k$ ) reproduces this trend. The weighted degree ( $w$ ) on the contrary shows a strong decrease, disclosing a tendency to differentiate the investments. This may be a response to the crisis: more fragmentation of production to diversify the risk and reorganize the production.

The two clustering coefficients have a different trend as can be easily explained.  $cc1$  (measuring the links between the first neighbors) is almost constant;  $cc2$  (considering links between both first and second neighbors) is strongly increasing in 2015 due to the emergence of few large clusters. This is evident from Fig. 4 and Fig. 5 that show the investor networks relatively to the year 2003 and 2015 respectively.

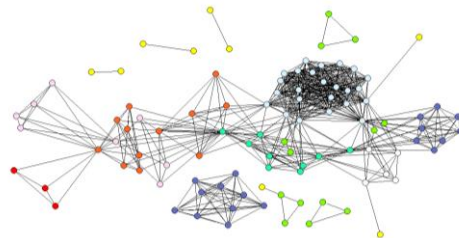


Fig. 4. Projected network on Investor space (year 2003)

A very relevant change of the structure emerges. While the number of investors is lower in 2003 and also forming clusters quite disconnected, in 2015 the number of investors strongly increase and they are tightly connected disclosing five large clusters.



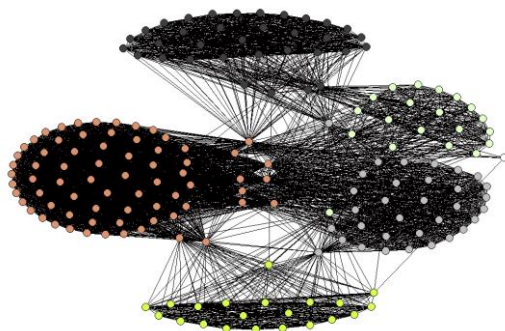


Fig. 5. Projected network on Investor space (year 2015)

Their maximum degree is really high (38 in 2003 and 146 in 2015) as well as their betweenness, indicating the tendency of these firms to invest worldwide. Moreover, sector leaders produce mechanical and electronic components and their projects are mainly related with manufacturing products, which have an intrinsic global spreading. Even if the identity of firms cannot be disclosed, each cluster is formed around a big firm (we can say a sector leader).

The projected network of companies reinforces what has already been seen for the destination countries. We have moved from a fairly disconnected network to a very connected one but with emerging clusters. These clusters are well identified by the k-core method. In Fig. 4 and Fig. 5 each cluster is identified by a different color. The clusters are quite well defined both for 2003 and 2015. In this sense the methodology proved to be very effective. This evidence of emerging clusters discloses a convergence in the strategies adopted by the companies in the sector that are concentrated in the same production regions. At a preliminary analysis, we can say that there is a convergence in the strategies adopted that primarily concern the identified markets. We also emphasize that cost reduction does not seem to be the main reason for these investments.

## V. CONCLUSIONS

In this paper the problem of fragmentation of production, one of the main emerging economic phenomena of last years, has been studied. Big data are nowadays available in order to study the investments of single firms in worldwide countries. Traditional analyses based on statistical distributions and their parameters as well as methods from Machine Learning and Big Data analysis are not enough to highlight the role of heterogeneity and to enhance the complex structure of interconnections. For this reason, we based our analysis on Complex Network approach. Unlike most traditional statistical techniques, this approach is relevant, because it allows discriminating between different agents, without canceling their differences as usual in averaging processes of traditional statistics. Indeed, agent's heterogeneity does play a crucial role in economic phenomena, that often can neither be predicted nor explained considering average representative economic agents. Most relevantly,

the economic connections between the economic agents inside the system are considered. In particular, economic failure propagation can be studied only considering the architecture of these connections. For instance, it is completely different on a random network or on a network characterized by hubs and peripheral nodes, like the real ones. This may play a crucial role in the study of economic vulnerability and systemic risk.

Moreover, network approach allows outlining the second order correlation and the cluster structure, not only looking to the first neighbors but also to other members of sub-networks and communities within the large network.

The first (2003) and last year (2015) of fDi Market database has been analyzed using Network theory, with focus to European countries investing worldwide. Comparing the two years, we observe a change from a slightly connected network to a strongly connected network with very well defined clusters emerging in 2015 within the same industrial sector. K-core analysis allowed to identify the main clusters, each one driven by a sector leader. This is an evidence of convergence to common strategies of groups of different firms concentrated in the same production regions.

In the future, we plan to study the evolution of the network year by year focusing on different sectors, in order to outline the main differences in the fragmentation of production strategies and how they have been affected by the economic crisis.

## REFERENCES

- [1] D. Blazquez and J. Domenech, "Big data sources and methods for social and economic analyses," *Technological Forecasting and Social Change*, vol. 130, 2018.
- [2] M. Dehmer, F. Emmert-Streib, S. Pickl, and A. Holzinger, *Big Data of Complex Networks*, CRC Press, Francis and Taylor, 2016.
- [3] S. N. Dorogovtsev and J. F. F. Mendes, *Evolution of Networks*, Oxford University Press, 2003.
- [4] F. Schweitzer, G. Fagiolo, D. Sornette, F. Vega-Redondo, A. Vespignani, and D. R. White, "Economic networks: The New challenges," *Science*, vol. 325, no. 5939, pp. 422-425, 24, July 2009.
- [5] G. Iori, G. De Masi, O. Precup, G. Gabbie, and G. Caldarelli, "A network analysis of the Italian overnight money market," *J. Economic Dynamic and Control*, vol. 32, no. 1, pp. 259-278, 2008.
- [6] G. De Masi, Y. Fujiwara, M. Gallegati, B. Greenwald, and J. E. Stiglitz, "Japanese financial credit networks, evolutionary and institutional economics review," vol. 7, no. 2, pp. 209-232, 2011.
- [7] S. Battiston, D. Delli Gatti, M. Gallegati, B. Greenwald, and J. E. Stiglitz, "Credit chains and bankruptcy propagation in production networks," *J. Economic Dynamic and Control*, vol. 31, no. 6, pp. 2061-2084, June 2007.
- [8] D. Garlaschelli, S. Battiston, M. Castri, V. D. P. Servedio, and G. Caldarelli, "The scale-free topology of market

- investments,” *Physica A*, vol. 350, no. 2-4, pp. 491-499, May 15, 2005
- [9] G. Fagiolo, T. Squartini, and D. Garlaschelli, “Null models of economic network: The case of the world trade web,” in *Proc. Laboratory of Economics and Management (LEM), Sant’Anna School of Advanced Studies*, Pisa, Italy, 2011.
- [10] R. S. Wall and G. A. van der Knapp, “Sectoral differentiation and network structure within contemporary worldwide corporate networks,” *Economic Geography*, vol. 87, no. 3, pp. 267-308, 2011.
- [11] L. Alfaro and M. Chen, “The global network of multidimensional firms,” *Journal of International Economics*, vol. 94, no. 2, pp. 263-276, 2014.
- [12] G. De Masi, G. Giovannetti, and G. Ricchiuti, “Network analysis of Italian foreign direct investments,” *Physica A*, vol. 392, pp. 1202-1214, 2013.
- [13] C. Joyez, “On the topological Structure of Multinational network,” *Physica A*, vol. 473, pp. 578-588, 2017.
- [14] G. De Masi and G. Ricchiuti, “The network of european outward foreign direct investment,” Chapter contribution to book “Networks of International Trade and Investment: “Understanding globalisation through the lens of network analysis”, Vernon Press, edited by Alessia Amighini, Sara Gorgoni, Matthew Smith, 2018
- [15] L. C. Freeman, “A set of measures of centrality based on betweenness,” *Sociometry*, vol. 40, no. 35, p. 41, 1977.
- [16] G. Sabidussi, “The centrality index of a graph,” *Psychometrika*, vol. 31, pp. 581-603, 1966.
- [17] S. N. Dorogovtsev, A. V. Goltsev, and J. F. F. Mendes, “k-Core organization of complex networks,” *Physical Review Letters*, vol. 96, no. 4, 2006.
- [18] T. Kamada and S. Kawai, “An algorithm for drawing general undirected graphs,” *Inf. Process. Lett.*, vol. 31, no. 1, pp. 7-15, 1989.



**Giulia De Masi** received her PhD in Physics in 2007 on Statistical Properties and Dynamical Evolution of Complex Networks with Applications. Starting from her PhD, she focused on Statistical Modeling and Data Science with multidisciplinary collaborations, mainly in Engineering, Environmental Sciences and Economics. She has long experience both in University and Industry R&D sector. Her research interests include Complex Network analysis and modeling, Machine Learning and Data Science.



**Giorgio Ricchiuti** defended his PhD in Development Economics at the Università di Firenze (Italy). He is currently Associate Professor at the Università di Firenze and fellow of the Complexity Lab in Economics at Università Cattolica (in Milan). His research has been regarding dynamic models with heterogeneous agents and bounded rationality and, on how different modes of internationalization affect productivity and firms' survival probability.